QUANTITATION OF CALCIUM METABOLISM IN POSTMENOPAUSAL OSTEOPOROSIS AND IN SCOLIOSIS*

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Over the past several years, work by a number of investigators [reviewed in (1)] has led to the development of a kinetic approach to the study of Ca metabolism. Because the studies have not been numerous and because of differences in experimental technique, results and interpretations based on them have differed. For example, some investigators (2–5) failed to find a difference in Ca metabolism in patients with osteoporosis as compared with normal individuals, whereas others (6) report such differences.

The purpose of this report is to present findings in persons of different ages, including women with and without osteoporosis, and young people with scoliosis, studied before and after immobilization in a plaster cast. The findings were obtained by a consistent mode of analysis applied to data collected in a uniform manner. From the results, relationships have been derived between Ca absorption from the intestine and Ca deposition in bone, and between Ca deposition in and removal from bone. These relationships have been used to describe Ca metabolism as a system of interdependent vectors in dynamic equilibrium, and this description has been applied to postmenopausal osteoporosis and the events following immobilization.

METHODS

Table I summarizes the clinical data of the experimental subjects. The patients studied included four young patients with scoliosis, aged 14 to 23 years, and seven women, aged 41 to 74 years, four of whom had been diagnosed as having postmenopausal osteoporosis, whereas two of them were clinically normal. The seventh woman (Patient 20, Table I) appeared clinically normal and free of osteoporosis, although X-ray examination of her spine led to equivocal comment by the hospital roentgenologist. Roentgenologis-

cal characteristics of osteoporosis included wedging of spinal vertebrae, ballooning of discs, and increased radio-lucency of the spine. The clinical indications of scoliosis and the basis for and mode of surgical correction have been described (7–9).

The basic design of the studies was to admit a patient to the metabolic ward, measure his Ca balance, and carry out kinetic experiments with Ca45 or Ca47 at predetermined periods (see Appendix for details). Kinetic studies of the patients with scoliosis were generally done while the patients were ambulatory, 2 to 3 weeks after they had been placed in plaster jackets equipped with turnbuckles and while still in these jackets, and some months after they had recovered from an operation for spinal arthrodesis. Balance periods (lasting 15 to 21 days) encompassed the kinetic study periods (lasting 6 to 9 days). Patients with osteoporosis, or control subjects were studied according to a similar protocol, i.e., during control periods (without any treatment) and during periods when they were undergoing some treatment. The effect of various treatments will be the subject of a later report.

Before admission, patients were interviewed by a dietitian and also asked to keep a diet diary for a few days. On the basis of this information, a diet was devised that conformed to the usual nutrient intake of the subject. Diets consisted of three different individual menus that were rotated in order. Intake was controlled by weighing duplicate portions of all meals eaten and analyzing samples of the diet pools. When leftovers occurred, they were weighed, and the equivalent quantity was removed from the duplicate diet before pooling and subsequent analysis. The amounts involved were less than 5% of the Ca intake. While a kinetic study was in progress, urine and stool collections were on a 24-hour basis; otherwise, pooled 3-day (urine) or 6-day (stool) samples were collected.

Ca analysis was done by oxalate precipitation and titration with perchloratoceric acid (10). Urine was analyzed for Ca directly. The error of replicate analyses was held to $\pm 3\%$ SD. Feces and food were homogenized and converted to ash before analysis. The error of replicate analyses including conversion to ash was held to $\pm 5\%$ SD. Ca⁴⁵ analysis was done on samples of Ca oxalate (11) counted in an automatic flow counter (10). Ca⁴⁷ analysis was done in a scintillation well counter connected to a pulse-height analyzer and automated print-out device. The counting error on replicate samples was held to $\pm 5\%$ SD.

Data were analyzed according to the second of the two simplified methods, scheme I, previously described in detail (1). Specific activity data were expressed as the percent-

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Patient	Age	Sex	Wt	Clinical diagnosis and comments			
no.	years		kg				
1	41	F	49	Normal premenopausal woman			
2	59	F	52	Normal menopause 10 years ago; asymptomatic gallstones			
3	17	\mathbf{M} .	76	Scoliosis, congenital; idiopathic hypercalciuria			
4	16	F	48	Scoliosis, congenital			
7	74	F	54	Osteoporosis; hysterectomy 34 years ago; fractured ankle and neck of femur; number of compressions increased over the past 5 years of observation			
8	14	F	43	Scoliosis, idiopathic			
12	23	M	68	Scoliosis, idiopathic			
14	55	F	49	Osteoporosis; menopause 14 years ago; spinal arthrodesis 1 year ago			
18 OPD	69	F	56	Osteoporosis; menopause 23 years ago; on Nilevar* 1 or 2 X daily for 8 months before admission, but not while on study			
20	57	F	59	Osteoporosis?; hysterectomy 16 years ago; fibroids; cholecystectomy 7 years ago			
21	61	${f F}$	58	Osteoporosis; menopause 20 years ago			

TABLE I
Summary of pertinent clinical data

age administered dose per milligram Ca. Parameters of Ca metabolism were calculated in milligrams Ca (per day). The following symbols are used (see Figure 1): P = pool size, $v_T = \text{rate}$ of loss from pool, $v_u = \text{urinary}$ Ca output, $v_f = \text{endogenous}$ fecal Ca output, $v_F = \text{total}$ fecal Ca output, $v_a = \text{Ca}$ absorbed, $v_i = \text{Ca}$ ingested, $v_{o+} = \text{bone}$ formation, $v_{o-} = \text{bone}$ resorption, $\Delta = \text{Ca}$ balance, and $\alpha = \text{percentage}$ of Ca absorbed.

RESULTS

The results for the normal and osteoporotic women are summarized in Table II, and for the young people with scoliosis, in Table III. Both tables show the balance data $(v_i, v_u, v_F, \text{ and } \Delta)$. Isotope data from which the remaining parameters $(P, v_T, v_f, v_{o+}, v_{o-}, v_2, \text{ and } \alpha)$ were cal-

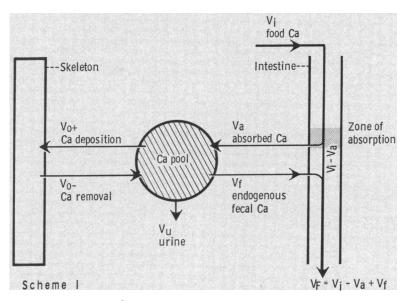


Fig. 1. Scheme of Ca metabolism depicting parameters evaluated in these studies.

^{*} 17α -Ethyl-19-nortestosterone.

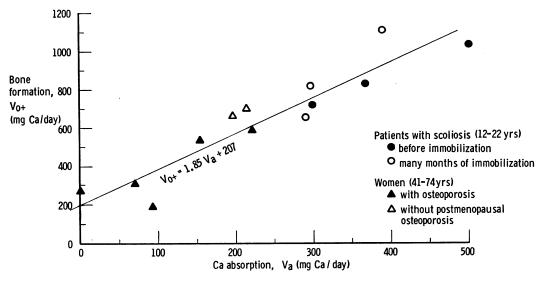


FIG. 2. RELATIONSHIP BETWEEN CA ABSORPTION AND BONE FORMATION. The equation was derived by the method of least squares and is based on all studies (Tables II and III) except 3B, 3D, 3F, 4D, 8C, and 12D.

culated are shown in the Appendix. The specific activity of the pool between 36 and 144 hours after injection of the isotope was determined from urine measurements. The equations for the time-course of the specific activity were derived by the method of least squares; the error of the individual values for slope and intercept was $\pm 5\%$.

The question arises whether relationships exist between the parameters of Ca metabolism in addition to those used to resolve the scheme. To put such relationships in evidence, we excluded all studies where either therapy had been instituted or a pathological condition existed. These conditions evidently could affect the system in dynamic equilibrium so as to constrain one or several parameters and produce a situation where normal regulation of Ca metabolism no longer prevails. The following studies were excluded: 3B, 3D, and 3F because the patient had idiopathic hypercalciuria, and 4D, 8C, and 12D because, as will be discussed below, the magnitudes of the parameters measured shortly after immobilization of these patients do not represent their norms.

Two relationships emerged; in one, Ca absorption and bone formation (in terms of unidirectional Ca loss from the pool) were linked by a linear relationship; in the other, a linear relation was found to exist between bone formation and bone resorption (expressed in terms of unidirectional Ca return to the pool).

TABLE II	
Ca metabolism data in women with and without postmenopausal	osteoporosis*

Study	P	v_T	v_u	v_F	v_f	v_{o+}	v_{o-}	v_i	Δ	v_a	α
	mg Ca				mil	ligrams C	a/day				%
21A	2,185	406	104	1,041	121	181	313	1,013	-132	93	9
14A	3,448	584	245	993	70	269	584	923	-315	0	0
20B	2,165	478	100	349	75	303	408	344	-105	70	20
18 OPD	2,089	922	263	298	123	536	768	329	-232	154	47
7A	3,086	792	66	707	139	587	569	791	+ 18	223	28
1B	3,424	855	171	558	33	651	658	722	_ 7	197	27
2A	4,950	998	206	495	94	698	783	616	- 85	215	35

^{*} Studies listed in ascending order of v_{o+} . $P=\text{pool size}, v_T=\text{rate of loss from } P, v_u=\text{urinary Ca output}, v_F=\text{total fecal Ca output}, v_f=\text{endogenous fecal Ca output}, v_{o+}=\text{bone formation}, v_{o-}=\text{bone resorption}, v_i=\text{Ca ingested}, \Delta=\text{Ca balance}, V_a=\text{Ca absorbed}, \text{ and } \alpha=\text{percentage of Ca absorbed}.$

Study	Immob. time	P	v_T	v_u	v_F	v_f	v_{o+}	v_{o-}	v_i	Δ	v_a	α
		mg Ca				mill	igrams Ca/	day				%
4C	Before	4,566	1,068	188	826	164	716	769	961	-53	299	31
4D	2 weeks	3,623	1,182	249	857	216	717	835	988	-118	347	35
4F	4 months	3,389	1,025	157	924	215	653	733	1,001	-80	292	29
8A	Before	3,968	1,428	199	483	198	1,031	927	786	+104	501	64
8C	6 weeks	5,000	1,476	443	548	167	866	1,049	808	-183	427	53
8E	5 months	3,676	1,129	234	455	78	817	733	773	+84	396	51
12B	Before	4,785	1,033	72	1,229	130	831	671	1,461	+160	362	25
12D	3 weeks	4,739	1,126	186	1,417	198	742	878	1,467	-136	248	17
12F	5 months	5,780	1,373	70	1,028	191	1.112	989	1,221	+123	384	31
3B	Before	6,098	1,624	331	862	187	1,106	1,140	1,159	-34	484	42
3D	4 months	3,831	1,066	392	1,115	118	556	988	1,075	-432	78	7
3F	9 months	5,586	1,461	351	912	66	1,044	1,237	1,070	-193	224	21

TABLE III

Ca metabolism data in patients with scoliosis*

Figure 2 pictures the relationship between Ca absorption and bone formation: $v_{o+} = 1.85v_a + 207$ (Equation 1), in milligrams Ca per day. The equation was derived by the method of least squares. The value of the slope (1.85) is highly significant (p < 0.01) as tested by comparing the linear regression variance with the deviation from this regression (F test). The 90% confidence limits of the slope are 2.27 and 1.43. The 90% confidence limits of the intercept are 322 and 92 mg Ca per day. Equation 1 indicates that v_{o+} and v_a varied in the same direction and that v_{o+} increased more rapidly than v_a . In-

spection of Figure 2 reveals that the older patients formed less bone and absorbed less Ca, whereas the values for the younger persons are located in the upper part of the curve, i.e., they formed more bone and also absorbed more Ca.

Figure 3 pictures the relationship between bone formation and bone resorption in these patients; the equation was derived by the method of least squares: $v_{o-} = 0.61v_{o+} + 298$ (Equation 2). The value of the slope (0.61) is highly significant (p < 0.01) as tested by comparing the linear regression variance with the deviation from this regression (F test). The

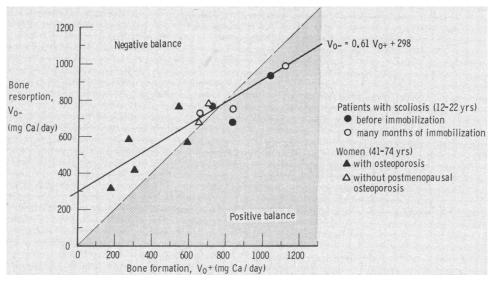


FIG. 3. RELATIONSHIP BETWEEN BONE FORMATION AND BONE RESORPTION. The equation was derived by the method of least squares and is based on the same studies as Figure 2. The dashed line represents $v_{0+} = v_{0-}$. The difference between the two lines is the Ca balance.

^{*} Symbols as in Table II.

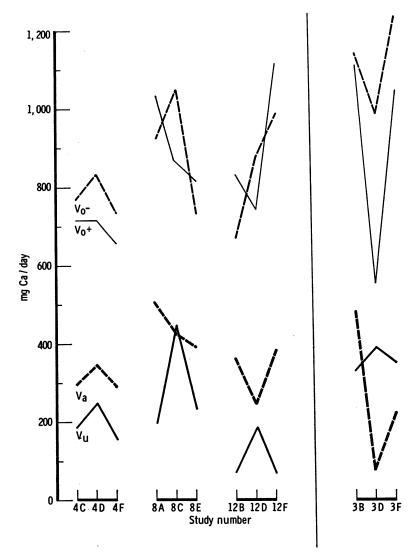


FIG. 4. EFFECT OF IMMOBILIZATION IN A PLASTER CAST ON CALCIUM METABOLISM IN FOUR PATIENTS WITH SCOLIOSIS. Patient 3 had idiopathic hypercalciuria. For explanation of studies, see Table III; $v_u =$ urinary Ca excretion, $v_a =$ Ca absorption, $v_{o+} =$ bone formation, and $v_{o-} =$ bone resorption.

90% confidence limits of the slope are 0.79 and 0.43. The 90% confidence limits of the intercept are 417 and 179 mg Ca per day.

Equation 2 indicates that v_{o+} and v_{o-} varied in the same direction, that v_{o-} increased less rapidly than v_{o+} , and that v_{o+} was greater than v_{o-} at values over 765 mg per day. This means that the probability of a person being in positive Δ when his v_{o+} exceeded 765 mg Ca per day was greater than when it was below that value. In the latter case, he would be expected to be in

negative Δ . This is shown graphically on Figure 3, where the dashed line represents the situation that would prevail if v_{o+} always equaled v_{o-} . Consequently, the difference between the experimental line determined by least squares and the line representing a zero Δ ($v_{o+} = v_{o-}$) is the predicted Δ . Inspection of Figure 3 also reveals that values measured for the younger persons are distributed along the upper portion of the curve, whereas those for the older persons are along the lower half.

The effect of immobilization in a plaster cast on certain of the parameters is shown graphically in Figure 4. The left-hand part of Figure 4 deals with three of the patients with scoliosis whose Ca metabolism appeared normal; on the right are pictured the changes in the patient with scoliosis who also had idiopathic hypercalciuria. In all four patients immobilization at first led to increased v_u , but after the patients had been in the cast for many months, values for v_u returned to their normal levels (12). In the three patients with normal Ca metabolism, the changes in v_a paralleled qualitatively the changes in v_{o+} . This suggests that the relationship represented by Equation 1 was not altered significantly as a result of immobilization; indeed, all values for v_{a+} and v_a fall within the error range $(\pm 1 \text{ SE})$ of Equation 1. This parallelism between v_{o+} and v_a also prevailed for Patient 3, but his values were outside the error range.

On the basis of Equation 2, v_{o+} and v_{o-} would be expected to vary in parallel. Figure 4 reveals that shortly after immobilization, v_{o-} increased in the three patients with normal Ca metabolism, whereas v_{o+} either decreased or remained the same. Qualitatively, therefore, the direction of change in these two parameters was different from normal. After the patients had been in the cast for some months, the relationship between v_{o+} and v_{o-} tended to return to what it was before immobilization, although the level was not always the same.

From the data reported here, no clear-cut distinction was possible between the control and the osteoporotic subjects, even though the parameters of the latter group tended to be low relative to the range of values observed in the entire group studied here (Tables II and III, Figures 2 and 3).

DISCUSSION

Dynamics of Ca metabolism. The various parameters of Ca metabolism measured and the supplementary relationships derived describe a complex system in a state of dynamic equilibrium whose vectors appear interdependent. The state of Ca metabolism of each subject studied has been defined in terms of this system, and some data, like Ca retention, have been expressed in

terms of their component rates and therefore have assumed greater physiological significance.

Because it was possible to define two independent relationships for v_{o+} , v_{o-} , and v_a (Equations 1 and 2), the entire system can be described for this group of subjects as a function of v_{o+} : $\Delta = 0.39v_{o+} - 298$ and $v_u + v_f = 0.15v_{o+} + 186$ (Equations 3 and 4). Equation 3 is obtained by substituting Equation 2 in the relationship $\Delta = v_{o+} - v_{o-}$, and Equation 4 by combining Equations 1 and 2 and substituting in the relationship $v_u + v_f + v_{o+} = v_a + v_{o-}$. For derivation of these relationships, see (1). Equations 3 and 4 are based on the same experimental values as Equations 1 and 2. The degree, however, to which the individual experimental points deviate from the theoretical straight line is a function of the error inherent in the particular measurement, i.e., Δ or $(v_u + v_f)$.

Equation 1 indicates that v_{o+} and v_a varied in the same direction, but does not indicate which was the independent variable. Another possibility is that both v_{o+} and v_a were functions of a third, independent factor. The possibility that under certain circumstances an insufficient amount of Ca may be absorbed to satisfy a relationship between v_{a+} and v_a has a bearing on the concept of Ca requirement. It is evident from Equation 1 that if v_{o+} is to be maintained at a certain level k, v_i cannot drop below (k-a)/b, if $\alpha = 100\%$ and where a is the intercept and b the slope for an equation such as Equation 1. Therefore, if v_{o+} were known for persons of varying ages and states, minimal Ca requirements could be set up. Tables II and III indicate that no obvious relationship existed between v_i and v_a , with α varying between 0 and 64%. Hence it proved impossible to derive a relationship between v_i and v_{o+} for the group of subjects studied

Equation 2 indicates that both skeletal metabolic processes, v_{o+} and v_{o-} , varied in the same direction. It does not indicate whether v_{o+} , or v_{o-} was the independent variable, or whether both were functions of a third factor. Since in our system of analysis (1) Δ is the difference between v_{o+} and v_{o-} , it follows from Equation 2 that Δ is a direct function of the intensity of v_{o+} , described for our subjects by Equation 3. If,

therefore, the relationships described by Equations 1 through 4 are maintained, a negative Δ will result if skeletal turnover is of relatively low intensity. In our group of patients, the older women who had a skeletal turnover of relatively low intensity fell into that category, although no clear-cut distinction could be made between the women with and those without osteoporosis. Nevertheless, in the light of the system of Ca metabolism just discussed, postmenopausal osteoporosis could be described as a condition where the intensity of most of the various parameters of Ca metabolism tends to be relatively low. Such a description implies that treatment of postmenopausal osteoporosis might profitably aim at increasing the turnover of the bone mineral. Whether this can be attained by increasing v_a as suggested by Nordin (13), or only by directly augmenting v_{o+} requires further study.

Immobilization in a plaster cast resulted, in all four patients, in a transitory change in the relationship of v_{o+} to v_{o-} , so that the difference between these two rates became larger than before and 4 to 9 months after immobilization. If this change were the result of an effect on skeletal metabolism without compensating changes in the remainder of the system, the pool would expand appreciably. If Ca homeostasis involves keeping P relatively constant, either losses from the pool must augment or entries diminish. Patients 4, 8, and 12 increased their v_u considerably, altering v_a relatively little. Patient 3, perhaps because he had idiopathic hypercalciuria. did not increase his v_u by much, but his v_a dropped profoundly. Undoubtedly a complete description of Ca homeostasis is more complex than the preceding statements imply. Nevertheless, these findings illustrate the different possibilities of regulating Ca metabolism, e.g., renal against intestinal control.

The fact that many months after these patients had been placed in the casts, their Ca metabolism tended to return to their respective norms implies that no permanent alteration had resulted from immobilization and spinal arthrodesis.

SUMMARY

By a combination of balance and isotope techniques, the following parameters of Ca metabolism were measured: pool size (P), rate of

loss from pool (v_T) , urinary excretion (v_u) , fecal excretion (v_F) , intake (v_i) , endogenous fecal Ca (v_f) , absorption (v_a) , balance (Δ) , bone formation (v_{o+}) , and bone resorption (v_{o-}) . The subjects were two normal women and five women with postmenopausal osteoporosis, aged 41 to 74 years, and four patients with scoliosis, aged 12 to 22 years. The latter were studied before, shortly after, and many months after immobilization in plaster casts.

From these data, the following relationships were derived: I) $v_{o+} = 1.85v_a + 207$ and 2) $v_{o-} = 0.61v_{o+} + 298$, and hence, 3) $\Delta = 0.39v_{o+} - 298$ and 4) $v_u + v_f = 0.15v_{o+} + 186$, in milligrams Ca per day. These equations indicate that in our patients all vectors of Ca metabolism could be expressed as a function of bone formation.

On the basis of these relationships, it appeared that the negative Ca balance observed in the older women was due to the low intensity of the various vectors of Ca metabolism, without clearcut distinction between the subjects with and without osteoporosis. Conversely, in the young patients with scoliosis, the negative balance incident to treatment by immobilization was associated with vectors of relatively high intensity whose relationships were altered temporarily.

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APPENDIX

Together with the balance data $(v_u, v_F, v_i, \text{ and } \Delta)$ reported in Tables II and III, the kinetic data listed here allow calculation of all remaining parameters for each study. The various methods of analyzing the data have been presented in detail (1). Most of the studies were done after iv injection of radioactive calcium and the results analyzed by the second of the simplified methods described in (1).

When radiocalcium was given intravenously, 5 to 10 μ c Ca⁴⁶ as CaCl₂ in sterile isotonic saline solution was injected into the arm vein. The Ca⁴⁶ was obtained as Ca-45-P-2¹

¹ U. S. Atomic Energy Commission, Oak Ridge, Tenn.

and was suitably diluted and sterilized in a rubber-capped vial. When Ca^{47} was used, 15 to 30 μc Ca^{47} as $CaCl_2$ was administered; it was diluted and prepared like the Ca^{46} . Standards were prepared by diluting to 100 ml with $CaCl_2$ solution (0.04 mg Ca per ml) an identical dose, withdrawn with the same syringe used for iv injection just before injection into the patient.

When the isotope was given by mouth, 10 to 20 μ c Ca⁴⁶ as CaCl₂ was injected into a glass of 150 to 180 g milk; the milk was thoroughly stirred and usually left in the refrigerator overnight. The patient drank the milk at midmorning, and the appropriate amount of Ca, or milk, or both was taken into account when preparing that day's menu. The standard was prepared like that in iv studies.

In the table below, A_4 and a_4 are the two experimental parameters of Equation A1, derived from urine specific activity values between 36 and 144 hours after isotope injection: $R_s = A_4 e^{-a_4 t}$, where R_s = the specific activity of the pool (% dose per mg Ca) and t = time in days. R_u and R_F are the amounts of radioactivity recovered in the urine and feces, respectively, during a period equivalent to 0 to 6 days; both are expressed in % dose.

In all these studies, vy was calculated by applying

$$v_f = v_u(R_F]_{t1}^{t_2}/R_u]_{t1}^{t_2}$$
. [A2]

In study 4C, R_F was recovered from days 0 to 4 only. Since radioactivity was administered by iv injection, results were analyzed by the simplified method; v_f was not calculated as above, but by:

$$v_f = v_T \times (R_F]_0^4 / [1 - e^{-a_4 t}]_0^4$$
. [A3]

The experimental data were: $A_4 = 0.0219$, $a_4 = 0.2340$, $R_u]_0^6 = 16.2$, and $R_F]_0^4 = 9.4$.

In study 14A, where R_F was known only for days 1 to 5, the data were treated as in study 4C; radioactivity was administered by iv injection and the experimental data were: $A_4 = 0.0290$, $a_4 = 0.1694$, $R_u \]_0^6 = 30.1$, and $R_F \]_1^5 = 5.0$.

Study	A_4	a 4	R_u	R_F
1B	0.0292	0.2496	18.6	3.5
2A	0.0202	0.2016	17.5	5.2
3B	0.0164	0.2664	19.3	10.9
3D	0.0261	0.2784	37.5	11.2
3F	0.0179	0.2616	24.1	4.5
4D	0.0276	0.3264	23.7	20.8
4F	0.0295	0.3024	13.7	18.8
7A	0.0324	0.2568	5.5	11.6
8A	0.0252	0.3600	17.0	16.9
8C	0.0200	0.2952	34.3	13.0
8E	0.0272	0.3072	24.1	8.0
12B	0.0209	0.2160	5.6	5.9
12D	0.0211	0.2376	14.1	15.2
12F	0.0173	0.2376	4.2	11.4
20B	0.0462	0.2208	15.7	11.1

Study 18 OPD was analyzed by the radioactivity balance method (1): radioactivity was administered by mouth. The experimental data were: $A_4 = 0.0224$, $a_4 = 0.4416$, $R_W |_0^6 = 11.8$, and $R_F |_0^6 = 58.7$.

In study 21A, radioactivity was also administered by mouth. Results were analyzed by the simplified method, and v_f was calculated by Equation A2. In this case, R_f (which differs from R_F in an oral experiment) was obtained by analyzing the monoexponential portion of the feces specific activity curve. The experimental data were: $A_4 = 0.00421$, $a_4 = 0.1860$, $R_u
bracket_2^6 = 0.903$, and $R_f
bracket_2^6 = 1.051$.

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